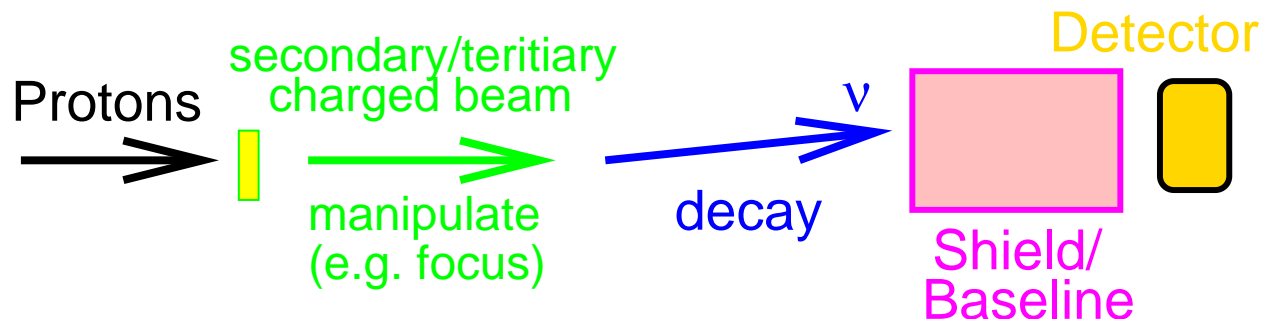


Why Muon Decays?



“Conventional” ν beams are produced by

$$\pi^+ \rightarrow \mu^+ \nu_\mu$$

$$\tau_{\pi^\pm} \sim 25 \text{ ns}$$

Muon decays

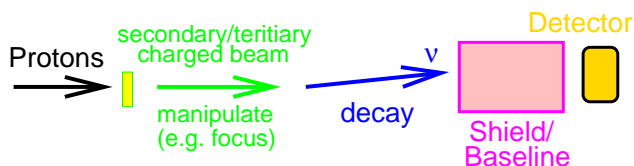
$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$$

$$\tau_\mu \sim 2 \text{ } \mu\text{s}$$

$\pi^+ \rightarrow \mu^+ \nu_\mu$	$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$
Can focus, but large emittance	Time to cool and focus
$Q \sim 34 \text{ MeV}$	$Q \sim 105 \text{ MeV}$
$\nu_\mu, \bar{\nu}_\mu$ only	$\nu_\mu, \bar{\nu}_\mu, \nu_e, \bar{\nu}_e$

Neutrino Detection Rates

Neutrino event rates depend
on a relatively small
number of factors



- Parent decays
- Neutrino beam divergence
(“spot size” at the detector)
From parent decay kinematics,

$$N_\nu \propto \frac{1}{\langle \theta_\nu \rangle^2}, \quad \langle \theta_\nu \rangle = \frac{\pi}{4\gamma_{\text{parent}}}$$

- Neutrino energy

$$\sigma(\nu N \rightarrow \ell^\pm X) \propto G_F s$$

- “Baseline”, i.e. distance to detector
(may be determined by physics goals)

$$N_\nu \propto \frac{1}{L^2}, \quad L \text{ large}$$

Muons as a source potentially win in
decays, divergence and energy
due to long lifetime!

Beam Divergence

Key difference between conventional and muon source is optimization of tradeoff of **parent production rates** and **beam divergence**

Conventional (π^\pm) Beam Economics

- **Production rates** fall steeply with increasing E_π
(production cross-section, proton acceleration)
- $N_\nu \propto N_\pi E_\pi^3$
(neutrino cross-section, divergence)

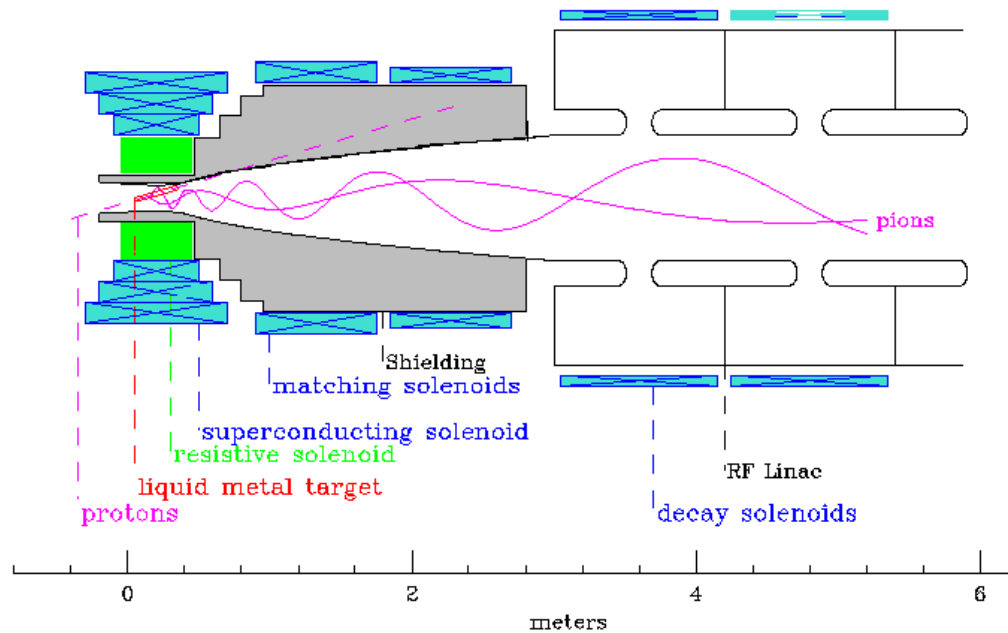
μ Beam Economics

- **Produce** and capture at low energies
(large cross-section, higher p power)
- **Accelerate parent beam** after **cooling**
 $N_\nu \propto (N_\mu E_\mu^3)$

Benefits are great...

...so can it be done?

A Resounding “Maybe”



Requirements

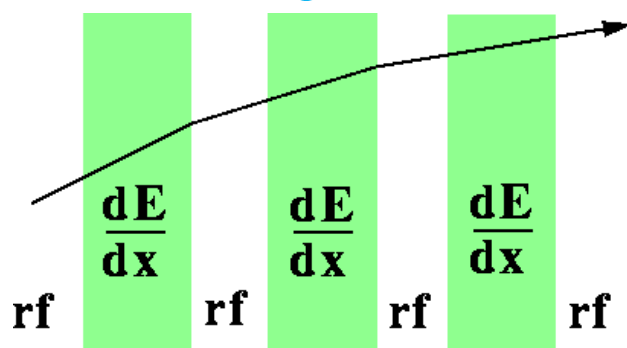
- **Very intense proton source**
 $\mathcal{O}(10^{14})$ protons, 15 Hz, 1 ns bunches
 (S.D.Holmes *et al.*, FERMILAB-TM-2021)
- **Pion Capture**
 - ▷ Collection efficiency: $0.6 \pi^+$ per proton
 - ▷ $p_z \sim p_t \sim 200$ MeV
 - ▷ $\sigma(\Delta E/E) \approx 1$
 - ▷ ...and then it decays to muons
- Left with a very **large muon beam**

A Resounding “Maybe” (cont’d)

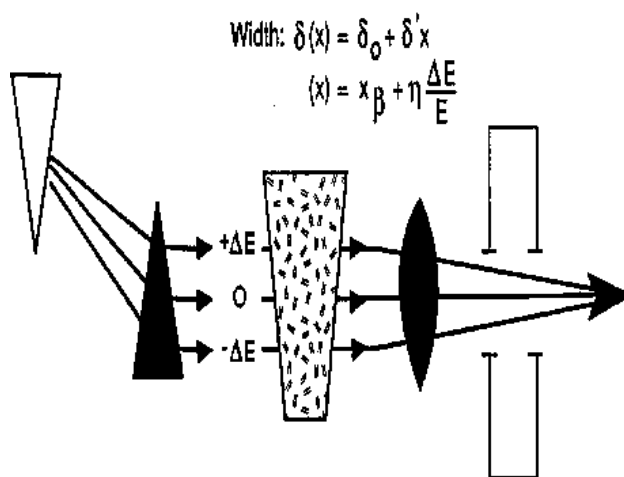
Hot muon beam \longrightarrow storable muon beam

- Cool *via* multiple scattering alternating with longitudinal acceleration

“Ionization Cooling” (Skirnsky and Parkhomchuk, 1981)



- Strong focusing needed

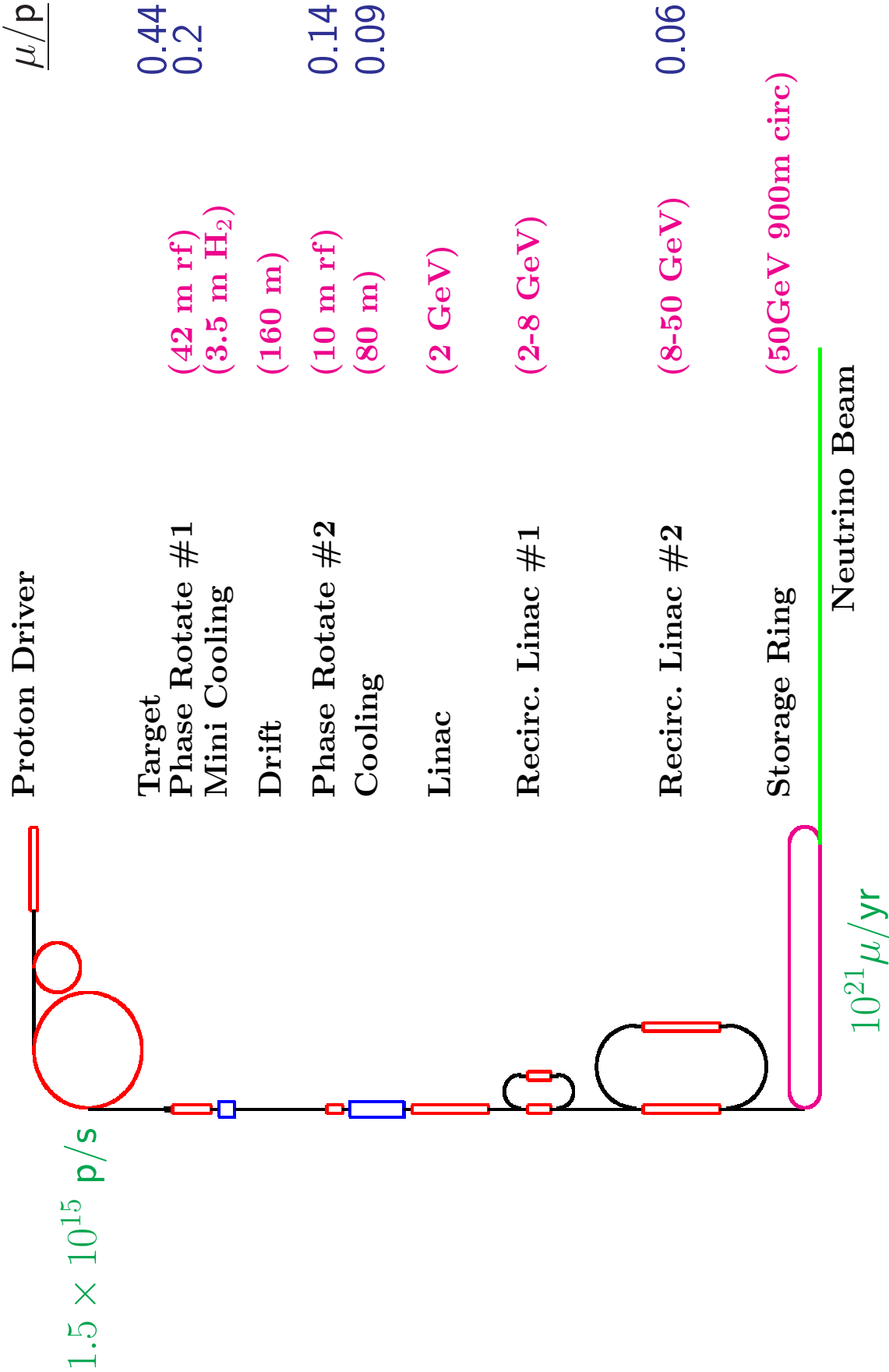


- Transverse emittance \longrightarrow longitudinal emittance

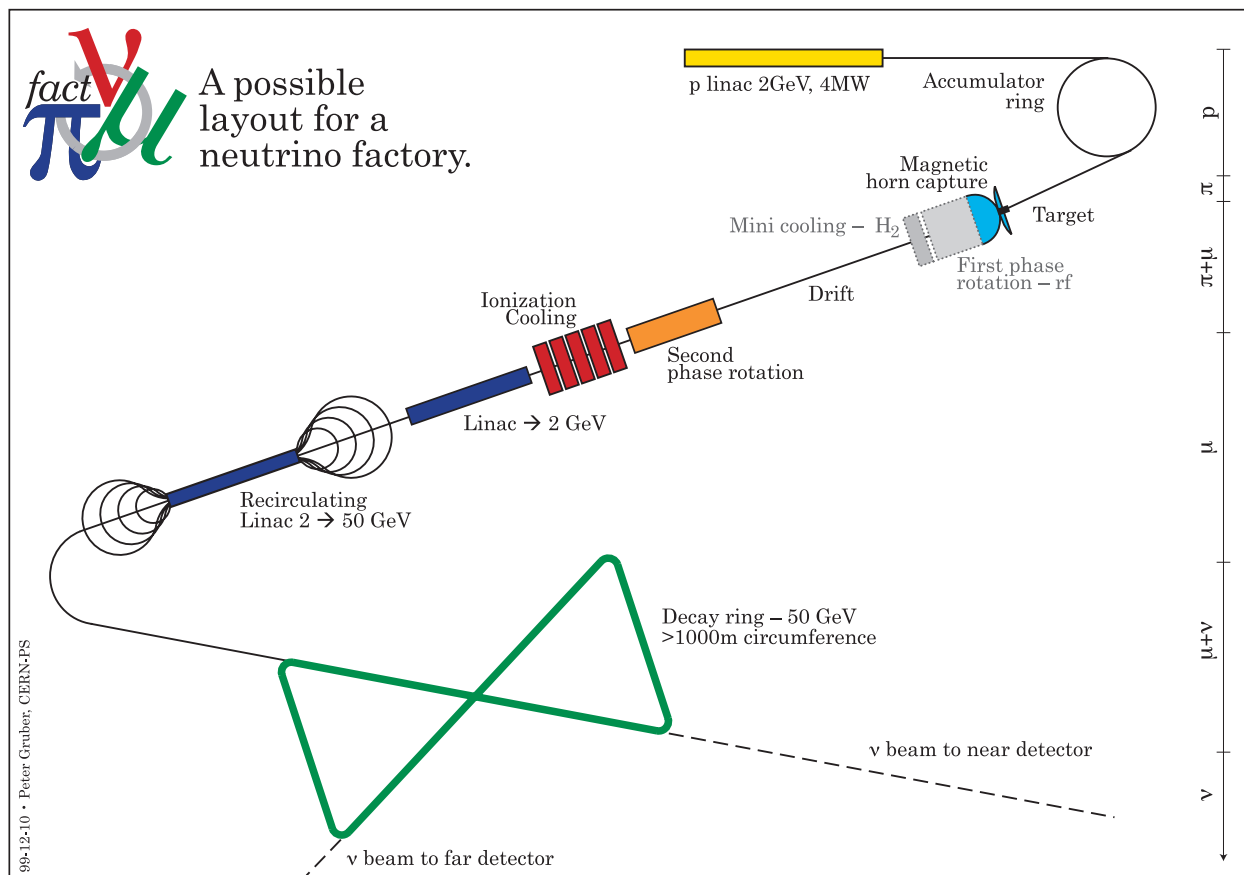
MUCOOL R&D program:

http://www.fnal.gov/projects/muon_collider/cool.html

A “generic” neutrino factory design



“Neutrino Factory” Design (cont’d)



- NSF initiative through Neutrino Factory and Muon Collider Collaboration

http://www.cap.bnl.gov/mumu/mu_home_page.html

- Active Accelerator, Detector and Physics working groups at FNAL and CERN

<http://www.fnal.gov/projects/muon Collider/>

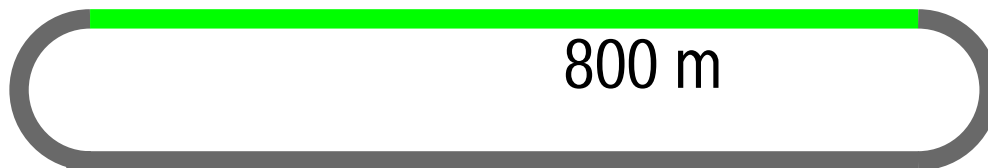
<http://muonstoragerings.cern.ch/Welcome.html/>

- All contributions to working groups welcomed!

Expected Neutrino Rates

Assumed Parameters (FNAL study group)

- $10^{20}/\text{yr}$ μ decays in the green straight section \Rightarrow



50 GeV

c.f.: Competing facilities

Beam	$\langle E_\nu \rangle$ [GeV]	ν per year
NuTeV/CCFR (Fermilab)	100	$\sim 10^{14}/\text{m}^2$
CHORUS/NOMAD (CERN)	30	$\sim 3 \times 10^{15}/\text{m}^2$
MINOS Near (Fermilab)	15	$\sim 10^{17}/\text{m}^2$
Neutrino Factory	30	$5 \sim 10^{19}/\text{m}^2$

Highly intense beams can...

- Contend with $1/L^2$
 - ▷ Long-baseline neutrino oscillations
- Or defeat small G_{FS} .
 - ▷ High rate neutrino experiments

Goals of Neutrino Oscillation Studies at a Neutrino Factory

In 10 years time...

- LSND will be confirmed/refuted. If confirmed, could know δm_{12}^2 to 0.1eV^2 , and $\sin^2 2\theta_{12}$ to 10%
- K2K & MINOS will confirm/refute atmospheric neutrino anomaly ($\nu_\mu \rightarrow \nu_\tau$)
- SuperK & MINOS may rule out $\nu_\mu \rightarrow \nu_{\text{sterile}}$
(Estimate δm_{23}^2 known to 30%, $\sin^2 2\theta_{23}$ to 20%)
- SNO & Borexino will determine if solar $\nu_e \rightarrow \nu_{\text{sterile}}$
Perhaps (with SuperK, KAMLAND) can determine correct solar solution

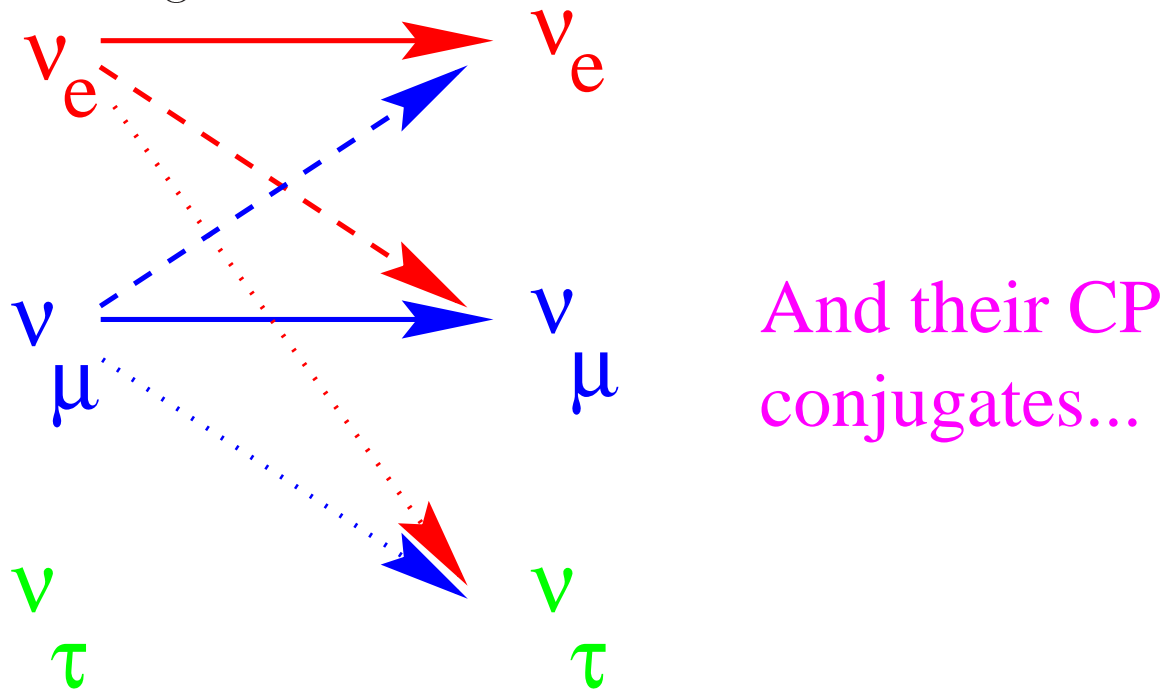
Most likely scenario: there will be 3 or more confirmed generations contributing to oscillations.

Remaining Questions to answer:

- Is 3-generation mixing matrix unitary?
- How is the mass hierarchy arranged?
- Is there CP violation?
- Observation of matter effects in accelerator beam?
- If sterile neutrinos: how many?

Muon Storage Ring Capabilities

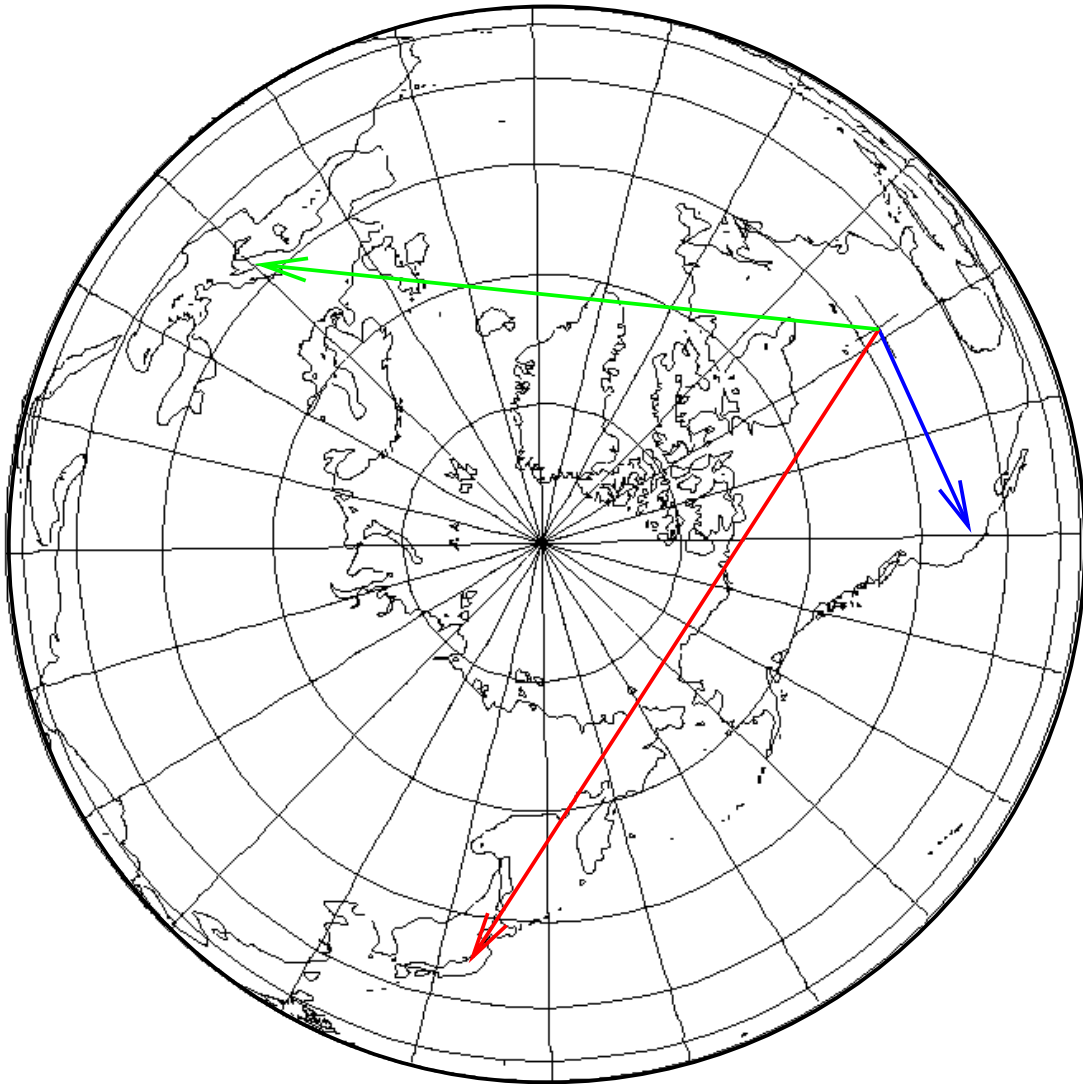
Looking for these flavor transitions



And looking for transitions from competing processes

- Three-generation oscillations
- Oscillations and matter transitions

Ideas for Neutrino Oscillation Experiments



30 GeV Neutrino Beams

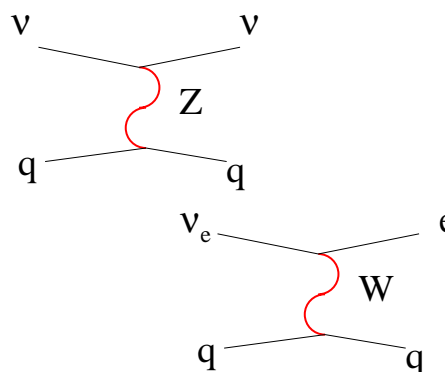
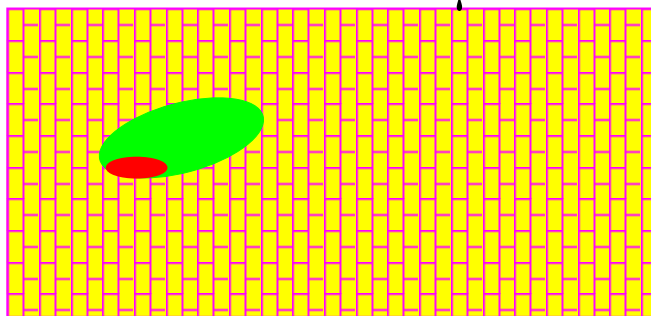
Baselines of few or many thousand kilometers

International Collaboration

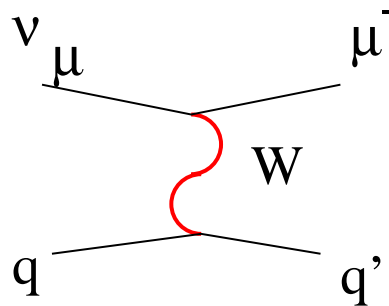
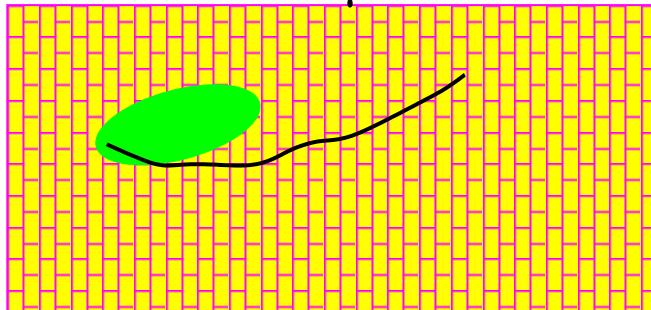
Most Simple Experiment: Wrong Sign Muons

Large (kTon) magnetized sampling/tracking calorimeter

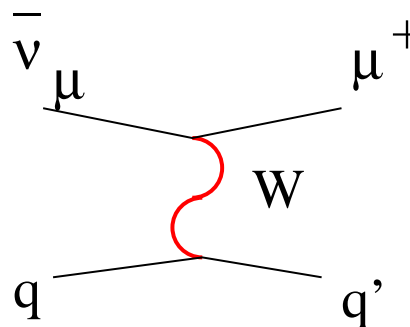
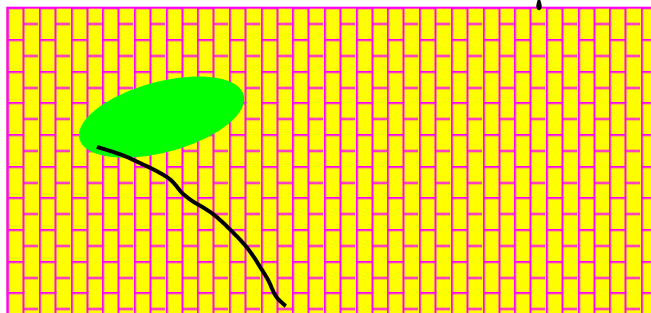
NC and CC $\bar{\nu}_e, \nu_\mu \rightarrow \nu_e$



CC ν_μ

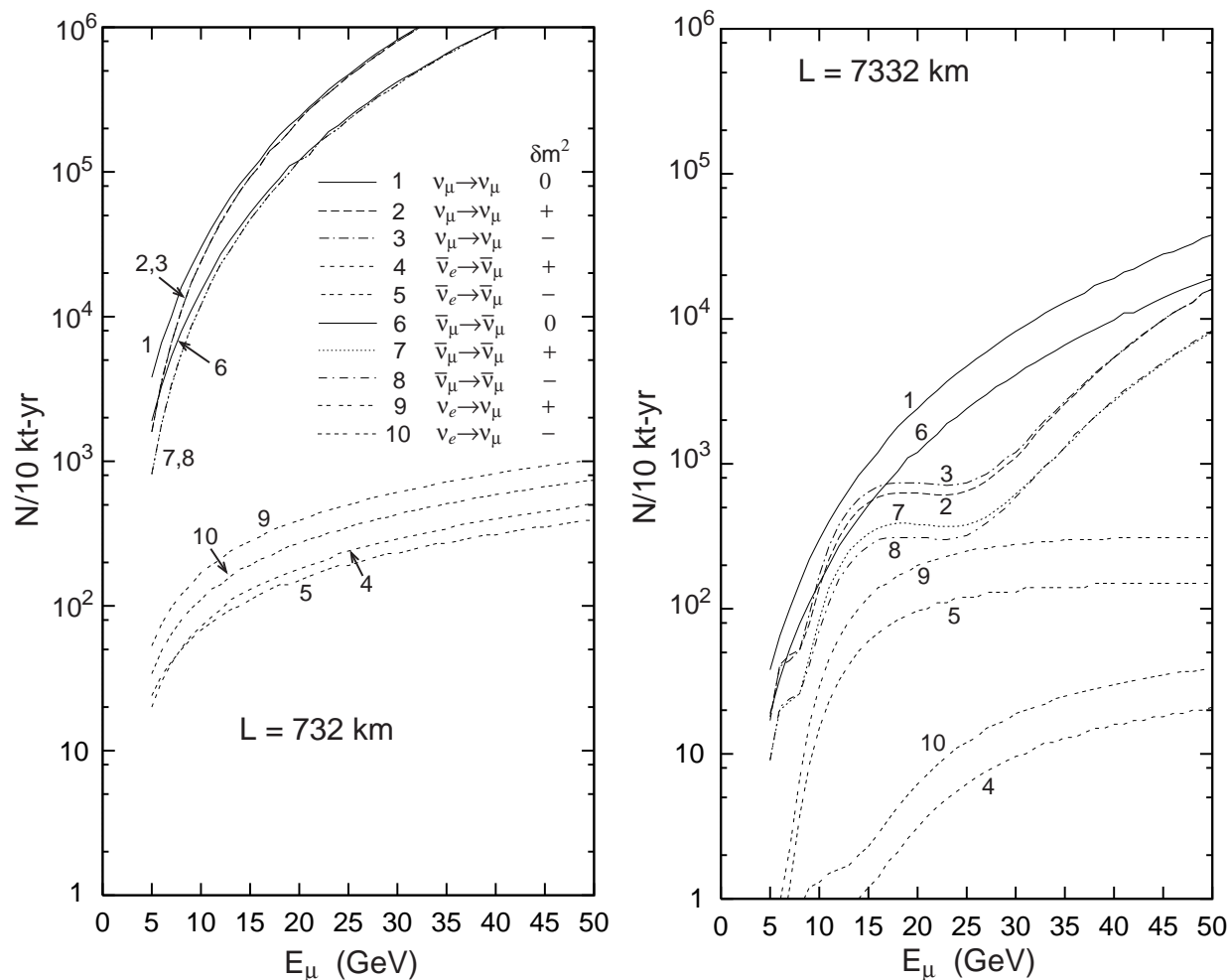


CC $\bar{\nu}_e \rightarrow \bar{\nu}_\mu$



Wrong-sign muon appearance is distinctive signature

Fermilab \rightarrow Soudan or Gran Sasso?



$$\sin^2 2\theta_{13} = 0.04, |\delta m_{21}^2| = 5 \times 10^{-5} eV^2$$

$$|\delta m_{32}^2| = 3.5 \times 10^{-3} eV^2$$

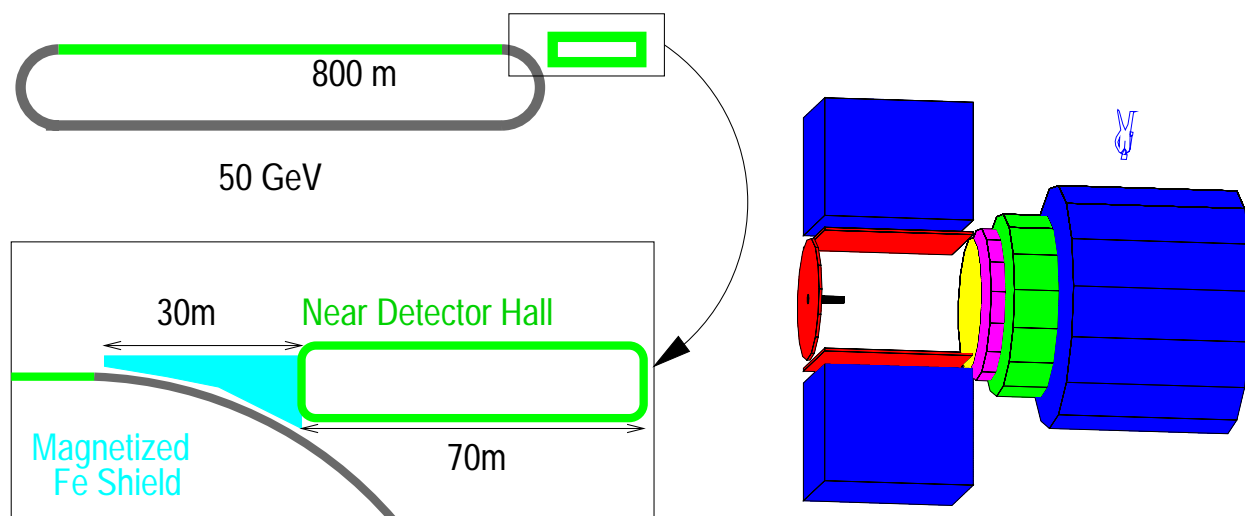
(V. Barger, S. Geer, R. Raja, K. Whisnant, [hep-ex/9911524](#))

- May want multiple baselines simultaneously
- Messy details like **backgrounds** are key in optimizing experiment...

High Rate Neutrino Experiments

$10^{20}/\text{yr}$ μ decays in the green straight section \Rightarrow

- 5–8% of all interactions within $r < 10$ cm
- 40–50% of all interactions within $r < 50$ cm
- $1.5\text{--}3 \times 10^6 \times \frac{E_\mu}{50 \text{ GeV}}/\text{kg}/\text{yr}$ at beam center



(multi-purpose detector design of B. King)

Small targets open up new possibilities in

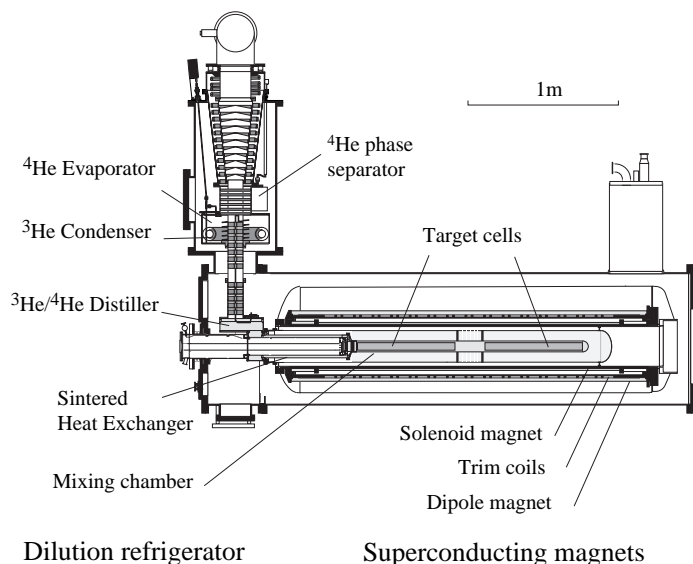
- **Target material**
- Final state detection

\Rightarrow New physics opportunities

Nucleon Structure at a Neutrino Factory

Why use neutrinos to probe nucleon structure?

- xF_3 : separate sea and valence
- Flavor tagging
 - ▷ $\nu s \rightarrow \mu^- c, c \rightarrow X \ell \nu$ tags strange quarks
 - ▷ $\nu d \rightarrow \mu^- u$ but $\bar{\nu} u \rightarrow d \mu^+$
 - ▷ $\nu c \rightarrow \nu^- c, c \rightarrow X \ell \nu$ (? hard...)
- High rate means we can wean νN from its addiction to heavy isoscalar targets
 - ▷ Polarized Targets?



- ▷ Solid Butanol, dilution factor of 0.1 (SMC)

Example: Polarized Target Experiment

(D. Harris, KSM)

Goal: Flavor-Separated Spin

$$\begin{array}{ll}
 \nu u \rightarrow \ell^- d & \nu \bar{d} \rightarrow \ell^- \bar{u} \\
 \bar{\nu} d \rightarrow \ell^+ u & \bar{\nu} \bar{u} \rightarrow \ell^+ \bar{d} \\
 \bar{\nu} s \rightarrow \ell^+ c & \nu \bar{s} \rightarrow \ell^- \bar{c}
 \end{array}$$

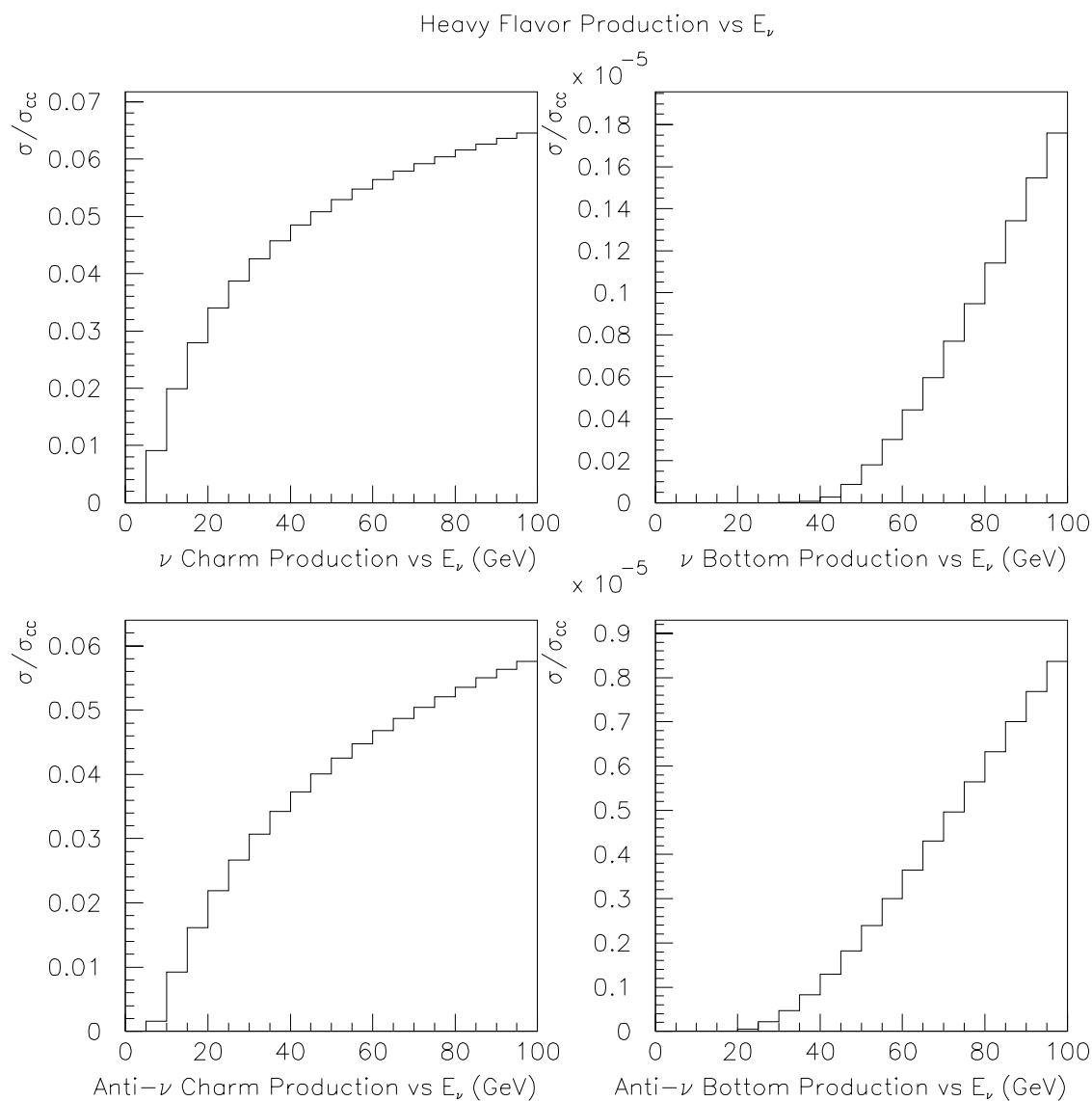
- q and \bar{q} from the inelasticity distributions
- $\nu/\bar{\nu}$ from lepton flavor

$\bar{\nu}(\nu)s(\bar{s}) \rightarrow \mu^\pm c(\bar{c})$ separated from $c \rightarrow \ell \nu X$ final states
 ($\sim 1\%$ of cross-section at 50 GeV)

\Rightarrow Measure strange sea polarization to $\sim 1\%$ precision
 (one year)

- Vastly superior flavor separation compared to hadron-based separation in HERMES

Neutrino Charm Factory: By-Products



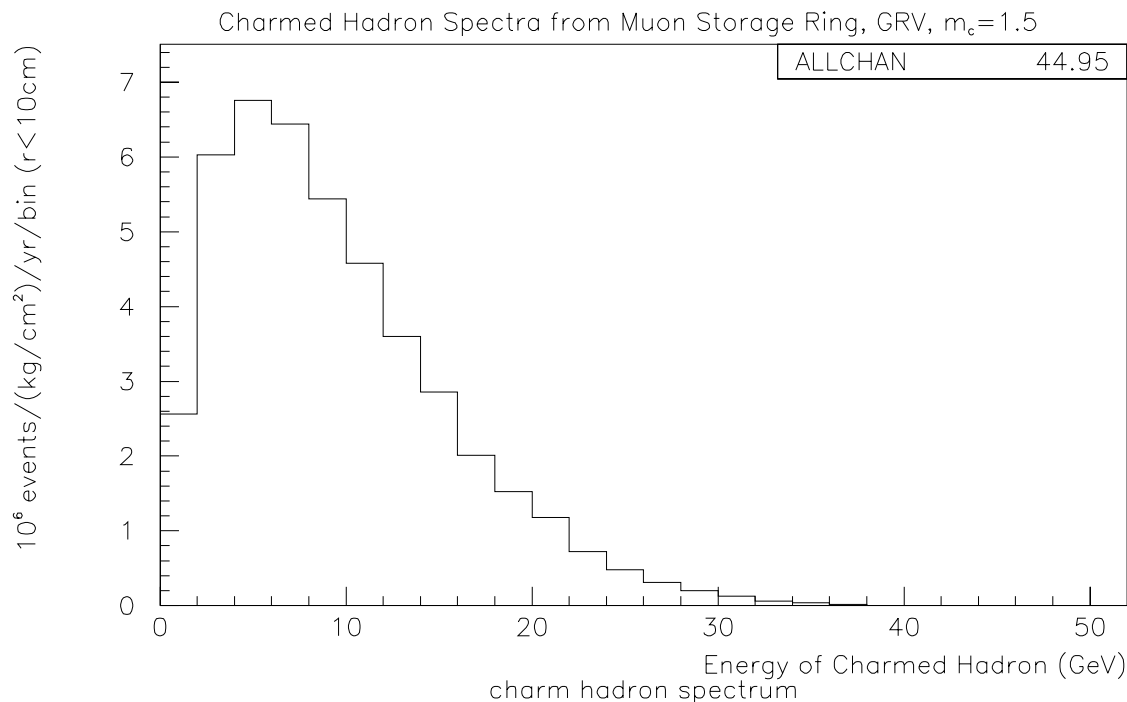
$$\frac{\sigma_{\text{charm}}}{\sigma_{CC}}$$

$$\frac{\sigma_{\text{bottom}}}{\sigma_{CC}}$$

- Charm Production averages $\approx 3\%$ of cross-section
- Bottom Production not accessible at 50 GeV
 - ▷ precise measure of $|V_{ub}|$ at high E_ν ? (B. King)

Neutrino Charm Factory II

- Charm spectrum is soft by fixed target standards
- Still, $10^5/\text{kg-yr}$ charmed hadrons above 10 GeV



- Rate is high; non-charm backgrounds relatively low
- Tagging
 - ▷ $\nu s \rightarrow \ell^- c$
 - ▷ $\bar{\nu} \bar{s} \rightarrow \ell^+ \bar{c}$
 - ▷ Tagging backgrounds are typically very low
 - * Most common mistag from $c \rightarrow \ell^+ X \nu$
(benign since charm is misreconstructed also)
- So what to do with $\sim 10^8$ tagged charm?

$D^0 - \bar{D}^0$ Mixing

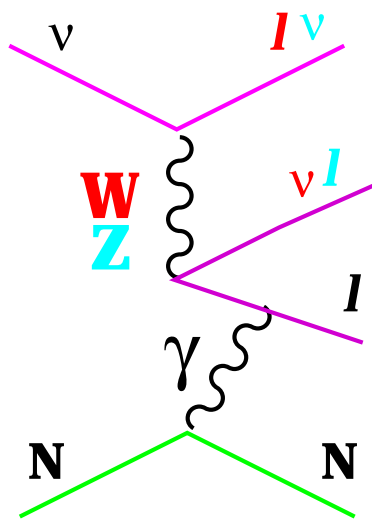
- $D^0 - \bar{D}^0$ is a clean signature of new physics if seen above 10^{-6} level
- e^+e^- and Fixed Target currently at $\text{few} \times 10^{-3}$ level (BaBar estimates $\text{few} 10^{-4}$ sensitivity with years at design luminosity)
 - ▷ Stuck on systematics/backgrounds
 - ▷ Reconstructed flavor from $D^0 \rightarrow K^- \pi^+$ (but $D^0 \rightarrow K^+ \pi^-$ is 1% of this rate)
 - ▷ Proper lifetime analysis required to get below 10^{-2}

One idea for $D^0 - \bar{D}^0$ Mixing in a Neutrino Factory Beam:

- High momentum lepton is tag
- Measure (inclusive) second lepton charge
 - ▷ about 30% from neutral D mesons
 - ▷ 10% efficient, assuming only e^\pm useful
 - * There is a $\text{few} \times 10^{-2}$ background from light meson decays in showers for the case of muons
 - ▷ probe 5×10^6 D^0 decays
- $D^0 - \bar{D}^0$ mixing gives $\ell_{\text{tag}}^\pm \ell_{\text{charm}}^\pm$
 - ▷ vs dominant $\ell_{\text{tag}}^\pm \ell_{\text{charm}}^\mp$

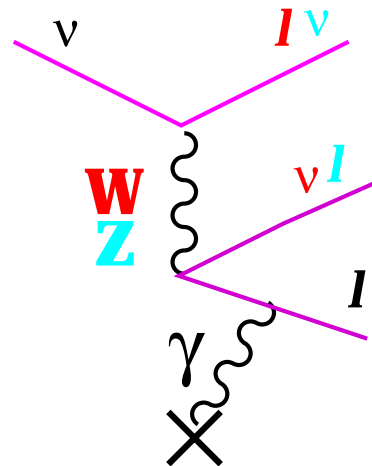
“External Tridents”

(A. Melissinos, KSM)



Nuclear form-factor leads to a large uncertainty in the cross-section

External field!
(well-determined, but weaker)



$$\sigma_{\nu\gamma} = \frac{\alpha G_F^2 s}{9\pi^2} \log \frac{s}{s_{\min}}$$

“External Tridents” (cont’d)

(A. Melissinos, KSM)

In an external magnetic field:

$$P_{\ell^+\ell^-} = \frac{\alpha G_F^2 s}{9\pi^2} \log \frac{s}{(2m_e)^2} \frac{B^2 E_\nu l}{2m_\ell^2}$$

For a 2 T, 10 m long field 20 cm in radius (50 GeV μ beam),

$$N_{e^+e^-} \sim 3 \times 10^3/\text{yr}$$

$$N_{\mu^+\mu^-} \sim 0.03/\text{yr}$$

- Signal is low mass, forward e^+e^- pairs from external field and nothing else
- High rate
- Needs a ν_e or $\bar{\nu}_e$ beam to test interference of W/Z terms (T. Bolton)
- Sensitive to anomalous $W\gamma$ or $Z\gamma$ couplings(?)

Direct Probes of Neutrino Properties

Some of the laundry list:

- Charge radius $\langle r^2 \rangle$ as an elastic form-factor or radiative emission
- Decays of heavy neutrinos with $m_{L^0} \sim 50$ MeV
 $m_{L^0} \rightarrow e^+ e^- \nu$
- Interaction/modification of ν beam in high external field
- ...

Why pursue these at a muon storage ring neutrino source?

- Roughly 10^4 increase in available neutrino fluxes

Conclusions

1. Exciting Times!

Accelerator R&D efforts are suggesting the possibility of high intensity, accelerated beams of muons

- Collimated, high rate ν_μ and ν_e beams

2. Long Baseline Oscillation Capabilities

- Probe CP violation, matter effects, unitarity of mixing matrix

3. Many high rate experiments supported by such a facility as well

- Interesting and diverse physics menu
- Surprises here?
- May attract a large experimental community